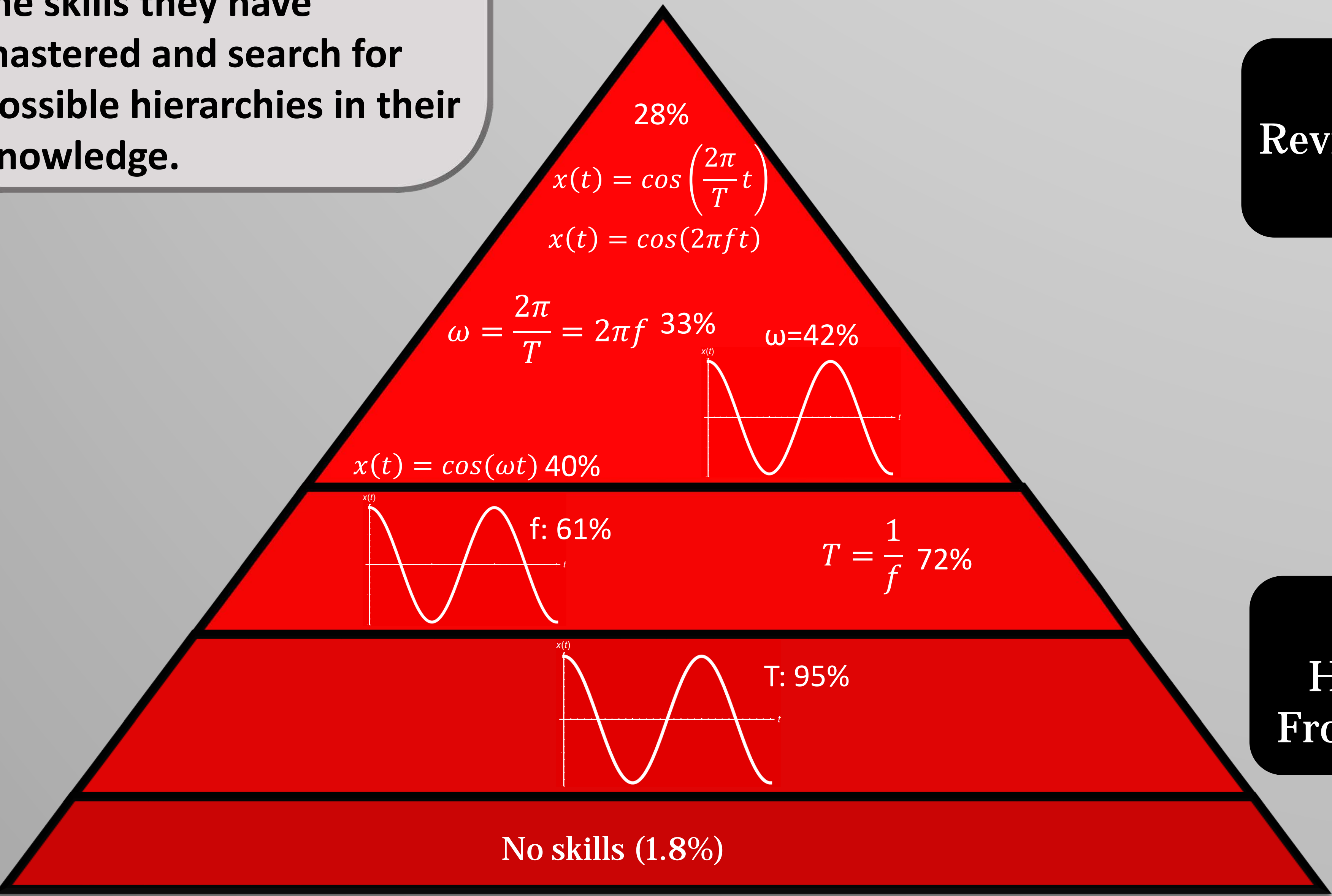


# Modeling Student Understanding of Period, Frequency, and Angular Frequency

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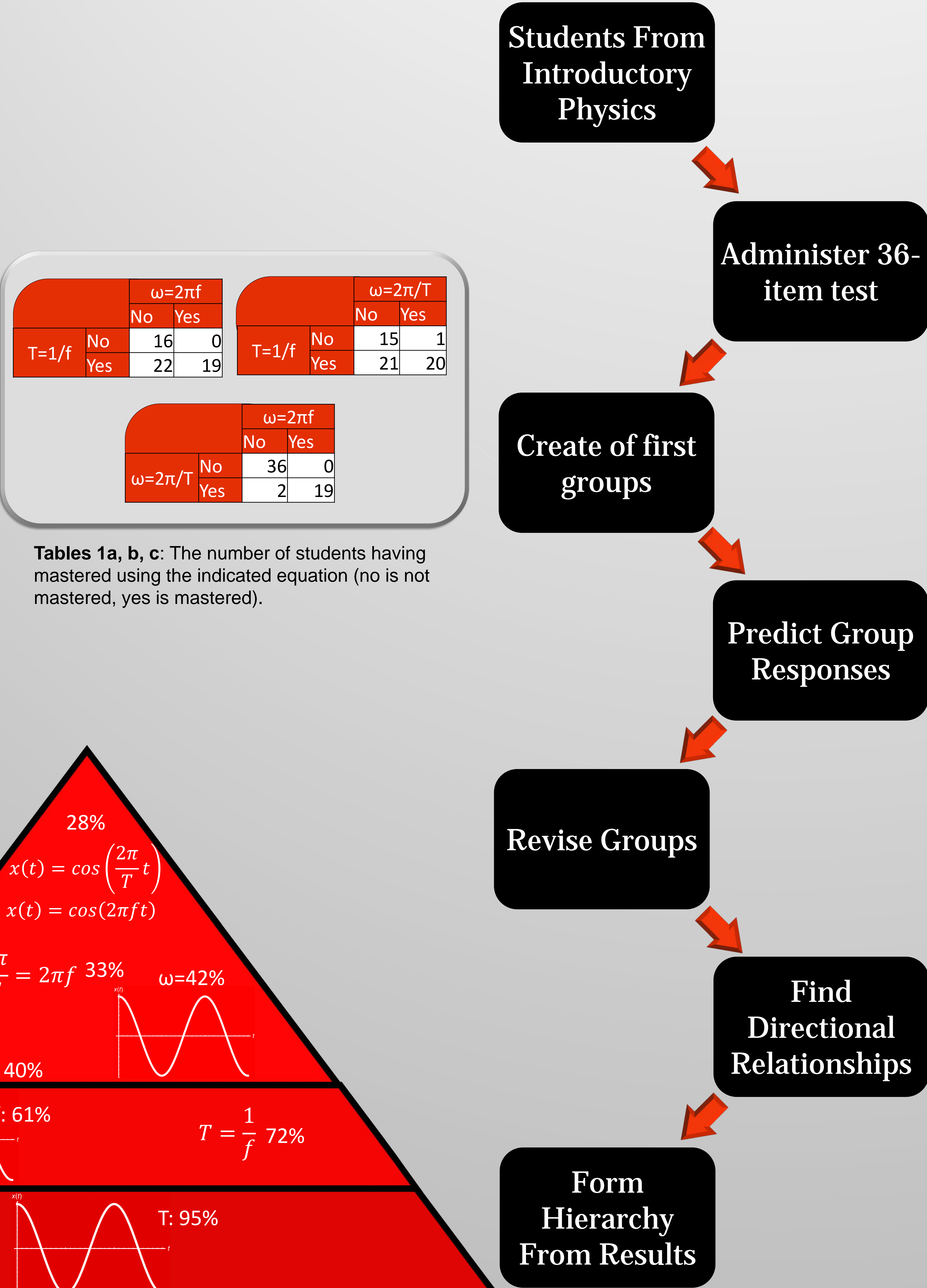
## Introduction

- Determining and understanding period, frequency, and angular frequency are essential skills and concepts in physics.
- Multiple representations are an important operational way of measuring skills and “understanding.”
- We previously found students have difficulty extracting information from graphical representations and have difficulty performing calculations involving the period (T), frequency (f), and angular frequency (ω).
- Goal: Classify student understanding according to the skills they have mastered and search for possible hierarchies in their knowledge.**



**Figure 3:** Hierarchy of skills related to determining the period, frequency, and angular frequency. Percent is the percentage of students having mastered the skill.

## Methodology/Results



		$\omega=2\pi f$	
		No	Yes
$T=1/f$	No	16	0
	Yes	22	19

		$\omega=2\pi/T$	
		No	Yes
$T=1/f$	No	15	1
	Yes	21	20

		$\omega=2\pi f$	
		No	Yes
$\omega=2\pi/T$	No	36	0
	Yes	2	19

**Tables 1a, b, c:** The number of students having mastered using the indicated equation (no is not mastered, yes is mastered).

What period is depicted in the following graph?

The equation  $x(t) = 7\cos(\frac{2\pi}{5}t + 3)$  describes the motion of a mass on a spring. What is the angular frequency of this motion?
 

A harmonic oscillator has a frequency of  $\frac{1}{4}$  Hz. What are the angular frequency and the period?

a. 4 seconds    b. 2 seconds  
 c. 1/4 seconds    d.  $\pi/2$  seconds

**Figures 1a-1c:** Sample graphical and equational questions and a sample calculation from the 36-item test.

		Graphical Questions					
		Period		Frequency		Angular Frequency	
Group		P	A	P	A	P	A
3 eqns	?	100%	✓	95%	✓	95%	✓
1 eqn	?	95%	✓	71%	✗	14%	✗
0 eqns	?	87%	✗	7%	✗	7%	✗

		Equational Questions					
		Angular Frequency		Period		Frequency	
Group		P	A	P	A	P	A
3 eqns	?	79%	✓	84%	✓	84%	✓
1 eqn	?	19%	✗	10%	✗	5%	✗
0 eqns	?	27%	✗	7%	✗	0%	✗

**Tables 2a and 2b:** Predicted (P) and actual (A) skills mastered by each group, where actual is the percent of students mastering the skill. A question mark signifies no prediction can be made from model.

Equation Period, Frequency	→	Equation Angular Frequency
Equation Period, Frequency	→	Graph Angular Frequency
Equation Period, Frequency	→	Graph Frequency
Equation Angular Frequency	→	Graph Frequency
Graph Frequency	→	$T=1/f$
$\omega=2\pi/T$ , $\omega=2\pi f$	→	Graph Frequency
$\omega=2\pi/T$ , $\omega=2\pi f$	→	$T=1/f$

**Figure 2:** Statistically significant relationships between mastered skills.

## Conclusions

- Student understanding of the period, frequency, and angular frequency can be modeled as a three-level hierarchy.**
- Less than half of the students at the top level, indicating a need for essential skills training.
- Understanding the period and frequency relationship is a prerequisite to understanding any relationship involving the angular frequency.
- Strong correlation between score on calculation questions and scores on graphical and equational questions

## Future Research

- Determine if students in introductory-algebra-based physics courses also display this hierarchical knowledge structure.
- Modify our Essential Skills platform to ensure that students master the period and frequency relationship before attempting to master any skill involving the angular frequency.

## Acknowledgements

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